

ΠΡΟΤΕΙΝΟΜΕΝΕΣ ΛΥΣΕΙΣ

ΘΕΜΑ Α

A1. →δ

A2. →β

A3. →α

A4. →γ

A5. α. → Σωστό

β. → Σωστό

γ. → Λάθος

δ. → Λάθος

ε. → Σωστό

ΘΕΜΑ Β

B1. → iii

ΘΕΜΑ Β

$$B1) \quad v = \lambda \cdot f \Rightarrow v = \frac{\lambda}{T} \Rightarrow \lambda = v \cdot T$$

$$x = (2k + 1) \cdot \frac{\lambda}{4} \Rightarrow L = (2k + 1) \cdot \frac{v \cdot T}{4}$$

• 2 δεσφοί άρα $k = 1$.

$$L = (2 \cdot 1 + 1) \cdot \frac{v \cdot T_1}{4} \Rightarrow L = \frac{3 \cdot v \cdot T_1}{4}$$

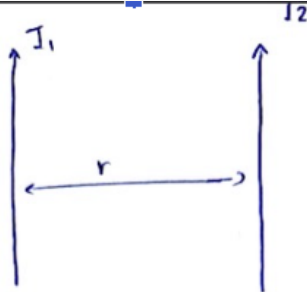
• 3 δεσφοί άρα $k = 2$

$$L = (2 \cdot 2 + 1) \cdot \frac{v \cdot T_2}{4} \Rightarrow L = \frac{5 \cdot v \cdot T_2}{4}$$

$$\text{άρα} \quad \frac{L}{L} = \frac{\frac{3 \cdot v \cdot T_1}{4}}{\frac{5 \cdot v \cdot T_2}{4}} \Rightarrow \boxed{\frac{T_1}{T_2} = \frac{5}{3}} \quad \textcircled{\delta}$$

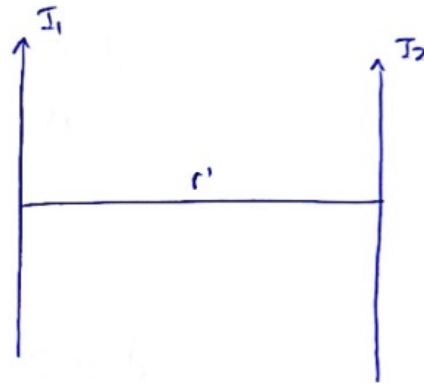
B2. → i

B2) $I_1 = I$
 $I_2 = 2I$



$$r' = d + r = \frac{r}{2} + r = \frac{3r}{2}$$

$$I_2' = 2I_2 = 4I$$



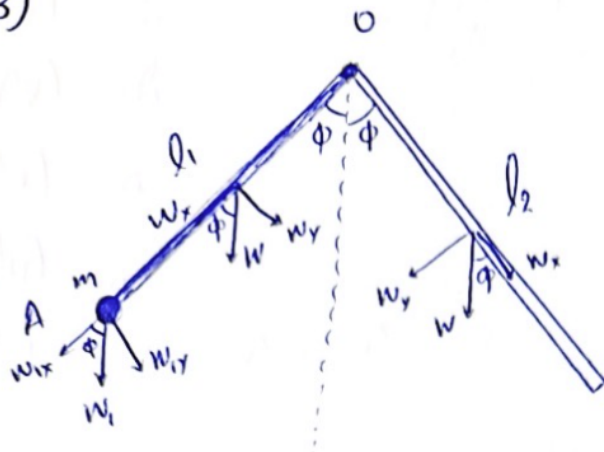
$$F_1 = \frac{\mu_0 \cdot I \cdot 2I \cdot \ell}{2\pi r} = \frac{\mu_0 I^2 \ell}{\pi r}$$

$$F_2 = \frac{\mu_0 \cdot I \cdot 4I \ell}{2\pi r'} = \frac{4\mu_0 I^2 \ell}{2\pi \cdot \frac{3r}{2}} = \frac{4\mu_0 I^2 \ell}{3\pi r}$$

Άρα $\frac{F_1}{F_2} = \frac{\frac{\mu_0 I^2 \ell}{\pi r}}{\frac{4\mu_0 I^2 \ell}{3\pi r}} \Rightarrow \boxed{\frac{F_1}{F_2} = \frac{3}{4}}$

B3. → ii

B3)



$$m = \frac{M}{2}$$

έχω ότι:

$$W = M \cdot g$$

$$W_1 = mg = \frac{Mg}{2}$$

$$W_1 = \frac{W}{2}$$

$$\sum \tau_O = 0$$

$$Mg \cdot \frac{l_1}{2} \cdot \eta \phi + W_1 \cdot g \cdot l_1 \cdot \eta \phi - Mg \cdot \frac{l_2}{2} \cdot \eta \phi = 0$$

$$Mg \cdot \frac{l_1}{2} \cdot \eta \phi + \frac{M}{2} \cdot g \cdot l_1 \cdot \eta \phi - Mg \cdot \frac{l_2}{2} \cdot \eta \phi = 0$$

$$\frac{2l_1}{2} \cdot \eta \phi + \frac{2l_1}{2} \cdot \eta \phi - \frac{2l_2}{2} \cdot \eta \phi = 0 \Rightarrow \boxed{\frac{l_1}{l_2} = \frac{1}{2}} \text{ (ii)}$$

ΘΕΜΑ Γ

$$\lambda = 8 \cdot \lambda_c \quad \lambda_c = \frac{h}{m_e \cdot c}$$

1. $\lambda' - \lambda = \frac{h}{m_e c} (1 - \cos \phi)$

$$\lambda' - \lambda = \lambda_c (1 - \cos 180^\circ)$$

$$\lambda' - \lambda = \lambda_c [1 - (-1)]$$

$$\lambda' - 8 \cdot \lambda_c = 2 \cdot \lambda_c$$

$$\boxed{\lambda' = 10 \cdot \lambda_c}$$

2. $E_\phi = h \cdot f = \frac{h \cdot c}{\lambda} = \frac{h \cdot c}{8 \cdot \lambda_c} = \frac{h \cdot c}{8 \cdot \frac{h}{m_e \cdot c}} = \frac{1}{8} m_e \cdot c^2$

$$E'_\phi = h \cdot f' = \frac{h \cdot c}{\lambda'} = \frac{h \cdot c}{10 \cdot \lambda_c} = \frac{h \cdot c}{10 \cdot \frac{h}{m_e \cdot c}} = \frac{1}{10} m_e \cdot c^2$$

$$K_e = E_\phi - E'_\phi = \frac{1}{8} m_e \cdot c^2 - \frac{1}{10} m_e \cdot c^2$$

$$K_e = \frac{1}{40} m_e c^2 = \frac{1}{40} \cdot 5 \cdot 10^5 \text{ eV}$$

$$\boxed{K_e = 12.500 \text{ eV}}$$

Γ₃. $\lambda_1 = 400 \text{ nm}$

$$\Phi = 1,4 \text{ eV} = 1,4 \cdot 1,6 \cdot 10^{-19} = 2,24 \cdot 10^{-19} \text{ J}$$

$$E_{\text{min}} = \Phi \Rightarrow h \cdot f_0 = \Phi \Rightarrow f_0 = \frac{\Phi}{h}$$

$$f_0 = \frac{2,24 \cdot 10^{-19}}{6,4 \cdot 10^{-34}} = 0,35 \cdot 10^{15} \text{ Hz}$$

Γ₄. $K_{\text{max}} = e \cdot V_0$

$$K_{\text{max}} = h \cdot f_1 - h \cdot f_0$$

$$e \cdot V_0 = h \cdot (f_1 - f_0)$$

χωρ. συ:

$$c = \lambda_1 \cdot f_1$$

$$f_1 = \frac{c}{\lambda_1}$$

$$f_1 = \frac{3 \cdot 10^8}{400 \cdot 10^{-9}}$$

$$f_1 = \frac{3 \cdot 10^8}{4 \cdot 10^{-7}}$$

$$f_1 = 0,75 \cdot 10^{15} \text{ Hz}$$

$$4,6 \cdot 10^{-19} \cdot V_0 = 6,4 \cdot 10^{-34} (0,75 - 0,35) \cdot 10^{15}$$

$$1,6 \cdot 10^{-19} \cdot V_0 = 2,56 \cdot 10^{-19}$$

$$V_0 = \frac{2,56}{1,6}$$

$$V_0 = 1,6 \text{ V}$$

ΘΕΜΑ Δ

ΔΕΝΑ Δ Στο σώμα ΝΛ

$$\Delta 1) \quad \Sigma F = 0$$

$$F - W_2 - T = 0$$

$$3 - 1 = T$$

$$\boxed{T = 2 \text{ N}}$$

$$W_2 = m_2 \cdot g = 0,1 \cdot 10$$

$$W_2 = 1 \text{ N}$$

Στο σώμα Μ1:

$$\Sigma F = 0$$

$$T - W_1 - F_{ελ} = 0$$

$$2 - 1 = F_{ελ}$$

$$\boxed{F_{ελ} = 1 \text{ N}}$$

$$W_1 = m_1 \cdot g = 0,1 \cdot 10$$

$$W_1 = 1 \text{ N}$$

$$x = m_1 \cdot \omega^2$$

$$10 = 0,1 \cdot \omega^2$$

οπότε

$$F_{ελ} = k \cdot x$$

$$1 = 10 \cdot x$$

$$\boxed{x = 0,1 \text{ m}}$$

$$\boxed{\omega = 10 \text{ rad/s}}$$

Άρα

$$A = \Delta l + x$$

$$A = 0,2 \text{ m}$$

Θ.Ι. του Μ1

$$\Sigma F = 0 \Rightarrow W_1 = F_{ελ} \Rightarrow$$

$$m_1 \cdot g = k \cdot \Delta l$$

$$\boxed{\Delta l = 0,1 \text{ m}}$$

Εφόσον το σώμα στα $t_0 = 0$ είναι στην αμείωτη

θέση έχει αρχική φάση $\phi_0 = \frac{\pi}{2} \text{ rad}$

$$\text{Άρα, } \boxed{x = 0,2 \cdot \eta \left(10t + \frac{\pi}{2} \right)}$$

D₂)

$$\frac{K}{\epsilon} = \frac{3}{4}$$

$$\frac{\epsilon - U}{\epsilon} = \frac{3}{4}$$

$$\frac{U}{\epsilon} = \frac{4}{4} - \frac{3}{4}$$

$$\frac{U}{\epsilon} = \frac{1}{4}$$

$$\frac{\frac{1}{2} K X^2}{\frac{1}{2} K A^2} = \frac{1}{4}$$

$$\frac{X^2}{A^2} = \frac{1}{4}$$

$$\left(\frac{X}{A}\right)^2 = \left(\frac{1}{2}\right)^2$$

$$\frac{|X|}{0,2} = \frac{1}{2}$$

$$|X| = \frac{0,2}{2}$$

$$|X| = 0,1 \text{ m}$$

$$a = \omega^2 \cdot X = 10^2 \cdot 0,1 = 10 \text{ m/s}^2$$

Α3) Ο αγωγός θα κινηθεί προς τα πάνω με επιταχυνόμενη κίνηση με συνεκώς κρούση επιτάχυνση και όταν ηδυνάμει η επιτάχυνση αρκεί μέγιστη ταχύτητα (U_p)

$$\Sigma F = 0$$

$$F - m_2 - F_L = 0$$

$$3 - 1 = F_L$$

$$F_L = 2 \text{ N}$$

$$B \cdot I \cdot l = 2$$

$$B \cdot \frac{B \cdot U_p \cdot l \cdot l}{R + R_{\text{ext}}} = 2$$

$$\frac{1 \cdot 1 \cdot U_p \cdot 1 \cdot 1}{1 + 1} = 2$$

$$\boxed{U_p = 4 \text{ m/s}}$$

$$\Delta 4. \quad \Delta t = 0,125 \text{ sec}$$

$$U_{\varphi} = 4 \text{ m/s}$$

$$U_{\varphi} = \frac{\Delta x}{\Delta t}$$

$$\Delta x = U_{\varphi} \cdot \Delta t$$

$$\Delta x = 4 \cdot 0,125$$

$$\boxed{\Delta x = 0,5 \text{ m}}$$

$$\bullet \quad W_F = F \cdot \Delta x$$

$$W_F = 3 \cdot 0,5$$

$$W_F = 1,5 \text{ J}$$

$$\bullet \quad Q = W_E = F_L \cdot \Delta x = 2 \cdot 0,5$$

$$Q = W_E = 1 \text{ J}$$

$$\pi \% = \frac{Q}{W_F} 100 \% = \frac{1}{1,5} 100 \% \approx 66,6 \%$$

Επιμέλεια Απαντήσεων:

Η Ομάδα του Ομίλου Ευκλείδη